

## X-intercepts, Multiplicities, and Y-intercepts

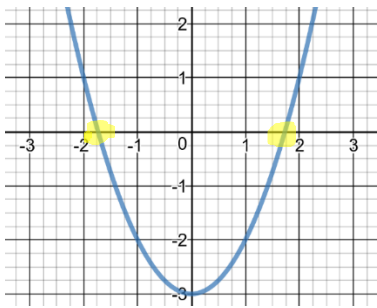
Like quadratics in standard form (which a quadratic is also a polynomial) the y-intercept is the constant since a y-intercept has the coordinate point (0,y); we simply substitute in 0 for all x values which will leave us with just the constant:

For example: the y-intercept of  $y = 5x^7 + 3x^5 - x^2 + 11$  is (0, 11). And if we are given the function graphically we simply look for where the graph crosses the y-axis.

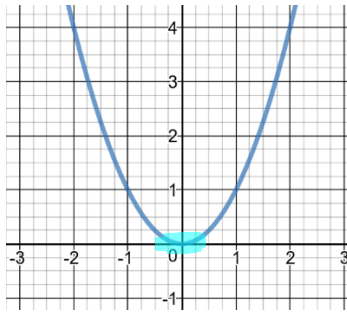
X-intercepts are a little harder especially algebraically (we will look at that a different time). Here you will only be asked to look at a graph and determine the x-intercepts.

For x-intercept look at where the graph crosses the x-axis. The number of x-intercepts is less than or equal to the degree of the polynomial

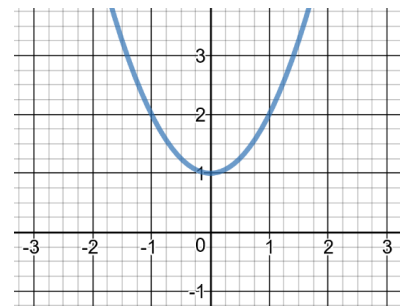
(# of x-int.  $\leq n$  where  $n$  is the degree)



This quadratic has **two real x-intercepts** which matches the degree.



This quadratic appears to have **one real x-intercept**; however, it gets **counted twice** (we just don't write it twice.  $y = x^2 = x \cdot x$  each x produces a zero just the same

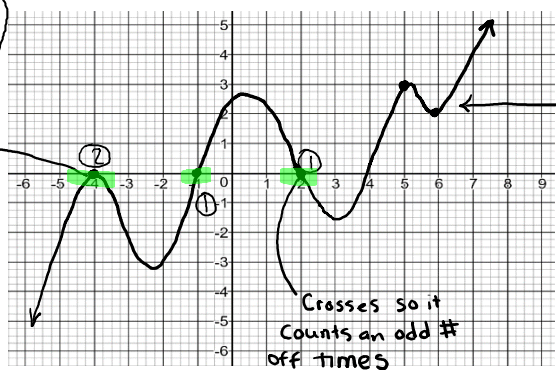


This quadratic has **no real roots**; however, it does have **two imaginary roots**. If we solved  $y = x^2 + 1$  we would produce an imaginary

Notice the number of roots whether real or imaginary add up to the degree.

What is **least possible degree**?  
 Answer: 3 from counting but could 5 because of imaginary.

Bounces  
 So it can count an even # of times  
 2, 4, 6, 8, 10, 12...



this is caused by imaginary roots so this will make it had to determine the degree.

1, 3, 5, 7, 9, 11...